

Ch 1.8 - Deductive Structure

Objectives:

- recognize **conditional** statements
- recognize the **negation** of a conditional statement
- recognize the **converse**, the **inverse** and the **contrapositive** of a statement
- Use the **chain rule** to draw conclusions

Agenda:

- 1) Take out HW to be checked
- 2) DO NOW
- 3) Logical Statements
- 4) Check in with Proofs - Peer Graded

HW: p. 47 #1- 9

Do Now:

Given the declarative statement "Two angles are both straight and congruent" identify the following:

Hypothesis (p): _____

Conclusion (q) : _____

Conditional Statement ($p \Rightarrow q$): _____

Converse Statement ($q \Rightarrow p$): _____

Is the converse a true statement? _____(yes or no)

If "no", provide a counter example: _____

Statements of Logic

1) Negation: The negation of any statement "p" is the statement "not p"

Notation: _____

ex. p = It is raining. $\sim p$ = _____

Statement	Example	T/F
Symbol		
Conditional	<i>If you live in Newton, MA, then you live in Massachusetts.</i>	<i>T</i>
$p \Rightarrow q$		
Converse		
	(If False) Counter Example	
Inverse		
	(If False) Counter Example	
Contrapositive		
	(If False) Counter Example	

Theorem: If a conditional statement is true, then the contrapositive of the statement is also true.

(If p then $q \Leftrightarrow$ If $\sim q$, then $\sim p$)

Chain of Reasoning: If $p \Rightarrow q$ and $q \Rightarrow r$, then _____

Ex. Consider the two statements:

If the team scores enough points, they will win the game.
(Notation _____)

And if they will win the game, the team goes to regionals.
(Notation _____)

And if the team goes to regionals, they will miss a day of school!
(Notation _____)

What can we conclude?

Lets revisit the "DO NOW" from yesterday and complete the following:

Given the declarative statement "Two straight angles are congruent" identify the following:

INVERSE Statement ($p \Rightarrow q$): _____

CONTRAPOSTIVE Statement ($q \Rightarrow p$): _____

Score _____/5

Name _____

Graded by _____

<p>1. Given: $\overline{FL} \cong \overline{AT}$ Prove: $\overline{FA} \cong \overline{LT}$</p>		
<u>STATEMENTS</u>		<u>REASONS</u>
1. _____		1. Given
2. $\overline{LA} \cong \overline{LA}$		2. _____
3. _____		3. Addition Prop of Equal.
4. _____		4. Segment Addition Property
5. $\overline{FA} \cong \overline{LT}$		5. _____

Score _____/5

Name _____

Graded by _____


<p>2. Given: $\angle AEB \cong \angle CED$ Prove: $\angle AEC \cong \angle BED$</p>		
<u>STATEMENTS</u>		<u>REASONS</u>
1. _____		1. Given
2. $\angle BEC \cong \angle BEC$		2. _____
3. _____		3. Addition Prop of Equal.
4. _____		4. Angle Addition Property
5. $\angle AEC \cong \angle BED$		5. _____

Score _____/5

Name _____

Graded by _____

1. Given: $\overline{FL} \cong \overline{AT}$
Prove: $\overline{FA} \cong \overline{LT}$



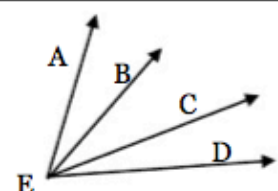
STATEMENTS	REASONS
1. $\overline{FL} \cong \overline{AT}$	1. Given
2. $\overline{LA} \cong \overline{LA}$	2. reflexive POE
3. $\overline{LA} + \overline{FL} \cong \overline{AT} + \overline{LA}$	3. Addition Prop of Equal.
4. $\overline{LA} + \overline{FL} = \overline{FA}$, $\overline{LA} + \overline{AT} = \overline{LT}$	4. Segment Addition Property
5. $\overline{FA} \cong \overline{LT}$	5. Transitive POE

Score _____/5

Name _____

Graded by _____

2. Given: $\angle AEB \cong \angle CED$
Prove: $\angle AEC \cong \angle BED$



STATEMENTS	REASONS
1. $\angle AEB \cong \angle CED$	1. Given
2. $\angle BEC \cong \angle BEC$	2. reflexive POE
3. $\angle AEB + \angle BEC \cong \angle CED + \angle BEC$	3. Addition Prop of Equal.
4. $\angle AEB + \angle BEC \cong \angle AEC$ $\angle CED + \angle BEC \cong \angle BED$	4. Angle Addition Property
5. $\angle AEC \cong \angle BED$	5. Transitive POE