

AGENDA

Objective: **SWBAT model and solve real-world problems involving exponential and logarithmic relationships**

Language Objective: **SWBAT answer reflection questions in writing in order to compare the graphs of exponential and logarithmic functions.**

- 1) Take out HW to be checked/DO NOW
- 2) HW Questions
- 3) Log Apps

HW: "Logs worksheet #6"

Do Now Solve for x.

1. $10 + \log_4 25 = x$

2. $4 + 4^x = 14$

3. $2 \cdot \log_3 x = \log_3(x-1) + \log_3 4$

4) You invest \$350 of your babysitting money into a savings account that earns 1.2% annually. How many years will it be until you have enough money to go on a vacation that costs \$600 (if you don't invest any more money into the account)?

Do Now Solve for x.

1. $10 + \log_4 25 = x$

$$10 + 2.32 = x$$

$$12.32 = x$$

2. $4 + 4^x = 14$

$$4^x = 10$$

$$\log_4(10) = x$$

$$1.66 = x$$

3. $2 \cdot \log_3 x = \log_3(x-1) + \log_3 4$

$$\log_3(x^2) = \log_3(4(x-1))$$

$$x^2 = 4x - 4$$

$$x^2 - 4x + 4 = 0$$

$$(x-2)(x-2) = 0$$

$$x = 2$$

4) You invest \$350 of your babysitting money into a savings account that earns 1.2% annually. How many years will it be until you have enough money to go on a vacation that costs \$600 (if you don't invest any more money into the account)?

$$600 = 350(1 + .012)^t$$

$$1.71 = (1.012)^t$$

$$\log_{1.012}(1.71) = t$$

$$44.98 = t \approx 45 \text{ years}$$

| | |
|--|--------------------|
| 1) Application: Suppose the number of lilies on a pond keeps doubling every week. It would take about 5000 lilies to cover a small pond and there are 2 lilies on the pond on the first day. How many lilies will be on the pond in 9 weeks? | 2) Equation |
| 3) What are we solving for? | 4) Solve |

| | |
|--|--------------------|
| 1) Application: Suppose the number of lilies on a pond keeps doubling every week. It would take about 5000 lilies to cover a small pond and there are 2 lilies on the pond on the first day. How many days will it take before the entire pond is covered? | 2) Equation |
| 3) What are we solving for? | 4) Solve |

| | |
|---|--|
| <p>1) Application: Suppose the number of lilies on a pond keeps doubling every week. It would take about 5000 lilies to cover a small pond and there are 2 lilies on the pond on the first day. How many lilies will be on the pond in 9 weeks?</p> | <p>2) Equation $A = 2(2)^9$</p> |
| <p>3) What are we solving for? <i>We are solving for the final <u>Amount</u> of lilies on the pond</i></p> | <p>4) Solve $A = 1024 \text{ lilies}$</p> |

| | |
|---|--|
| <p>1) Application: Suppose the number of lilies on a pond keeps doubling every week. It would take about 5000 lilies to cover a small pond and there are 2 lilies on the pond on the first day. How many days will it take before the entire pond is covered?</p> | <p>2) Equation $5000 = 2(2)^t$</p> |
| <p>3) What are we solving for? <i>We are solving for the number of days to reach 500 lilies</i></p> | <p>4) Solve $2500 = (2)^t$ $\log_2(2500) = t$ $11.29 = t \approx 11 \text{ days}$</p> |

| | |
|---|---------------------------|
| <p>1) Application: Suppose that a small country has a population of 10 million and an annual growth rate of 4.5%. How long will it take before the population doubles?</p> | <p>2) Equation</p> |
| <p>3) What are we solving for?</p> | <p>4) Solve</p> |

| | |
|--|---------------------------|
| <p>1) Application: A ball is dropped from a height of 25 feet and rises up two-thirds of that distance after its first bounce. Each succeeding height is two-thirds of the previous height. How many bounces must occur in order for the ball to bounce less than one foot from the ground?</p> | <p>2) Equation</p> |
| <p>3) What are we solving for?</p> | <p>4) Solve</p> |

| | |
|--|--------------------|
| 1) Application: The population of the United States was about 230 million in 1984. At an annual growth rate of 1.5%, how long, to the nearest tenth of a year, would it take for the population to grow 300 million? | 2) Equation |
| 3) What are we solving for? | 4) Solve |

| | |
|--|--------------------|
| 1) Application: Assuming that the Native Americans really did sell Manhattan for the legendary \$24, and further assuming that the sale took place exactly 388 years ago, how much money would the Native Americans now have if they had placed the money in a bank that paid 5% interest per year, compounded annually? | 2) Equation |
| 3) What are we solving for? | 4) Solve |

| | |
|---|--------------------|
| 1) Application: A particularly prolific microorganism has baffled all of modern science by dividing into 3 every hour. If there are 10 of these little bugs in a Petri dish at 9:00 one morning, how many will there be by 5:00 pm? | 2) Equation |
| 3) What are we solving for? | 4) Solve |

| | |
|---|--------------------|
| 1) Application: A particularly prolific microorganism has baffled all of modern science by dividing into 3 every hour. If there are 10 of these little bugs in a Petri dish at 9:00 one morning, after how many hours will there be 100,000 bacteria? | 2) Equation |
| 3) What are we solving for? | 4) Solve |

HW: "Logs worksheet #6"

Name _____ Date _____

M 518 Logarithms Applications

1. Explain why or when you need to use logs.

2. Write the equation in exponential form $\log_4 \frac{1}{16} = -2$ _____

3. Write the equation in logarithmic form. $x^t = z$ _____

4. Solve for x : (Do not need logs for this one...)

$$5^{4x} = 125^{x+6}$$

$x =$ _____

5. Solve each equation for x . If necessary, round your answer to the nearest hundredth.

a. $2 = \log_x 100$

b. $\log_{\frac{2}{3}} \frac{4}{9} = x$

c. $12^x = 500$

d. $8^{x+3} = 110$

6. Evaluate each expression.

a.* $\log_{12} 12^8 + \log_8 1$

b. $\log_2 \sqrt{2}$

c. $7^{\log_7 45}$

d. $\log_2 \frac{1}{4}$

e. $\log_{15} 200$

HW: "Logs worksheet #6" continued...

7. a) Find the amount of a \$3500 investment after 12 years at 5% interest compounded monthly. Round your answer to the nearest cent.

$$\text{Compound Interest Formula: } A = P\left(1 + \frac{r}{n}\right)^{nt}$$

b) Find out **when** the amount will reach \$4000. Round to nearest month. Must show work.

c) **When** will the amount double?

8. Bruce bought a car for \$12,000. The salesperson projected that the value of the car would decline by 14.5% per year for the next 6 years.

a. Write an expression for the projected value of Bruce's car after n years.

b. Predict the value, to the nearest hundred dollars, of Bruce's car after 6 years.

c. Find out after how many years and months will the car be half its value.